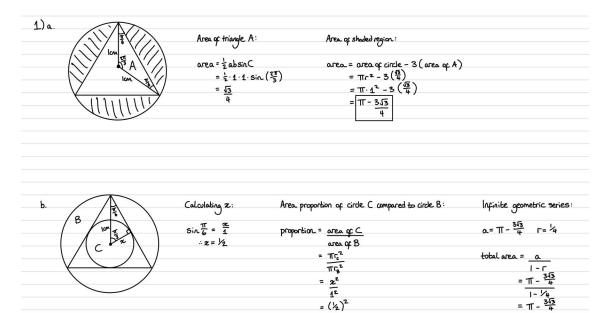
Interview 2 Answers

Question 1)



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Question 2)

2) a. Yes, with the following construction:

- b. No, lets think about how to construct ab from ab³ by applying these rules in <u>reverse</u>:

 If we start with a multiple of 3 bs (ab³) and can only abd 3 bs and half the number of bs, we will always have a multiple of 3 bs (halving a multiple of 3 results in a number that is also a multiple of 3).

 Hence, we can never reach ab, which does not have a multiple of 3 bs.
- c. Given a string $ab^n = ab^{2^k-3m}$, we can construct it in the following manner:

$$ab \xrightarrow{1} ab^{2} \xrightarrow{1} \dots \xrightarrow{1} ab^{2^{K}} \xrightarrow{2} ab^{2^{K}-3} \xrightarrow{2} \dots \xrightarrow{2} ab^{2^{K}-3m}$$

K times m times

d. Let us apply induction over the bose case (ab) and inductive cases (construction rules ax $\stackrel{1}{\rightarrow}$ axx and abblize $\stackrel{2}{\rightarrow}$ axx)

Base case:

$$u = ab = ab^{2^{\circ}-3(0)} = ab^{2^{\kappa}-3m}$$
 where $k = m = 0 \ (>0)$

Inductive hypothesis:

Assume a String u takes the form ab^{2K-3m} where K,m >0

Inductive cases:

$$u \stackrel{\cdot}{\rightarrow} u' : ab^{2^{k}-3m} \stackrel{\cdot}{\rightarrow} ab^{2^{k}-3m} b^{2^{k}-3m}$$

$$= ab^{2(2^{k}-3m)} \qquad u \stackrel{\cdot}{\rightarrow} u' : ab^{2^{k}-3m-3} b^{3} \stackrel{\cdot}{\rightarrow} ab^{2^{k}-3m-3}$$

$$= ab^{2^{k+1}} - 3(2m) \qquad \qquad bhere (k+1), (2m) \geqslant 0$$
where (k+1), (2m) \geq 0

Question 3)



as
$$\alpha \rightarrow +\infty$$
:

- $\cdot e^{\infty} \to +\infty$
- \cdot Sin(e^{lpha}) oscillates faster and faster between [-1,1]
- $y = \frac{\sin(e^x)}{e^x} \rightarrow 0$ (oscillating positive and negative)

as 2 → - 0

- $\cdot e^{\alpha} \rightarrow 0$
- · Sin $(e^{x}) \approx e^{x}$ (small angle approximation)

$$y = \frac{\sin(e^{x})}{e^{x}} \rightarrow \frac{e^{x}}{e^{x}} = 1$$

y=1------



So $y = \frac{\sin(e^x)}{e^x}$ looks like:

